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## **Existence Conditions for the Inconsistencies in the Databases Integration**

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**EXISTENCE CONDITIONS FOR THE  
INCONSISTENCIES IN THE DATABASES  
INTEGRATION**

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Technical report No. 760

June 1998

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**Abstract**

The technological progress in the areas of the hardware and the software, together with the general expansion of the computers to almost all human activities, make it easier to realize the integration of many already existing databases, would it be in order to build up the very fashioned data warehousing, an enterprise wide data store, or simply one of many types of distributed data base systems providing different kind of the interoperability in the form of various heterogeneous, federated or multi-database systems.

Unfortunately the process of the integration of (existing) databases can be accompanied by many various difficulties and problems. One of them is surely the possible occurrence of the inconsistencies appearing in this process of the integration.

In the report we study the existence conditions for these inconsistencies.

**Keywords**

database systems, logic, incomplete information

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# 1 Formulation of the Problem

We will study the conditions for the existence of the inconsistencies in the integration of several databases under the following natural logical assumption :

**A1** : *Each of the considered databases to be integrated has no inconsistencies ( when taken alone ) .*

Furthermore, for reasons of the simplification, and having in mind the current situation in the area of the database technologies where the **Codd relational data model** prevail, we will suppose that :

**A2** : *All the databases to be integrated are relational ones :*

Let  $\mathcal{B}_i$ ,  $i \in \widehat{m}$ , be  $m$  relational databases to be integrated ( $m \geq 2$ ), each consisting of  $k_i$  relations  $R^{i_j} = \langle A^{i_j}, D^{i_j}, T^{i_j} \rangle$ .

( See Appendix for definitions and notations )

Let us denote by  $\mathfrak{S}$  the set of all the possible *integrity constraints* over the given universe of discourse  $\mathcal{U} = \mathcal{D}(\mathbf{A})$  where :

$$\mathbf{A} = \bigcup_{i=1}^m \bigcup_{j=1}^{k_i} A^{i_j}$$

and

$$\mathcal{U} = \bigcup_{i=1}^m \bigcup_{j=1}^{k_i} D^{i_j}(A^{i_j})$$

and by  $\mathbf{I}$  a subset of the set  $\mathfrak{S}$ .

Let us further denote by  $\mathcal{R}(\mathbf{I})$  the set of all the relations over given universe of discourse satisfying  $\mathbf{I}$ .

We want to find the conditions which can lead to inconsistencies when trying to integrate some of the databases  $\mathcal{B}_i$ .

## 2 Integration by Unions of the Relations

We will suppose there exist ( at least two ) databases  $\mathcal{B}_{i_1}$  and  $\mathcal{B}_{i_2}$  each having ( at least ) one relation  $R^{i_j}_{q_j}$  of the same cardinality , say  $c$  ( greater or equal to two; if it was equal to one, the corresponding relations would be the lists, maybe ordered, which cannot lead to inconsistencies if the original relations had no inconsistencies ... ) :

$$\mathbf{A3} : (\exists c \geq 2) (\exists s \geq 2) (\forall j \in \hat{s}) (\exists \mathcal{B}_{i_j}) (\exists R^{i_j}_{q_j} \in \mathcal{B}_{i_j}) (|A^{i_j}_{q_j}| = c)$$

*Remark* : If all the databases  $\mathcal{B}_i$  do not consist of ( simple ) lists, we can always find, by successive projections, corresponding ( at least ) couples of (sub)relations  $R^{i_j}_{q_j}$  with the required properties.

First, for the simplification, we will suppose relations  $R^{i_j}_{q_j}$  are defined over the same relational scheme  $\mathbf{S} = \langle \mathbf{A}, \mathbf{D} \rangle$ , that is : 1.  $A^{i_j}_{q_j} = A$   
2.  $D^{i_j}_{q_j} = D$

$$\mathbf{A4} : (\forall j \in \hat{s}) (R^{i_j}_{q_j} \in S = \langle A, D \rangle)$$

We have shown in [Štuller, 1998] that the following hold :

$$\mathbf{Lemma 1} : ((\exists s \geq 2)(\forall j \in \hat{s})(\exists \mathcal{B}_{i_j})(\exists R^{i_j}_{q_j} \in (\mathcal{B}_{i_j} \cap \mathcal{R}(I)))) \not\Rightarrow (\bigcup_{j=1}^s R^{i_j}_{q_j} \in \mathcal{R}(I))$$

which can lead to inconsistencies ( of two different types : *data inconsistencies* and *integrity constraints inconsistencies* - see [Štuller, 1998] for details ) in the union.

But the union, to be meaningful, should be done only after a thorough semantical justification and verification because syntactical equality of attributes and of the corresponding domains may be misleading, especially in the case of overloaded concepts like *name*, *number*, *year* etc.

## 2.1 $\pi$ - unions

We can relax the condition that the relations we want to make an union over are defined over the same relational scheme by requiring the existence of the permutations

$\pi_{q_j}^{i_j}$  such that there exists the  $\pi$  - union of the relations  $R^{i_j}_{q_j}$  :

$$\mathbf{A5} : \quad \bigcap_{i=1}^s D^{i_j}_{q_j} (\pi^{i_j}_{q_j} (A^{i_j}_{q_j})) \neq \emptyset$$

If it is so, we can obtain the corresponding lemma for the  $\pi$  - union :

*Lemma 2 :*

$$((\exists s \geq 2)(\forall \mathbf{j} \in \hat{\mathbf{s}})(\exists \mathcal{B}_{i_j})(\exists R^{i_j}_{q_j} \in (\mathcal{B}_{i_j} \cap \mathcal{R}(\mathbf{I}))) \not\Rightarrow (\bigcup_{j=1}^s R^{i_j}_{q_j} \in \mathcal{R}(\mathbf{I})))$$

which can again lead to some inconsistencies ( apart from data and integrity constraints inconsistencies, mentioned before, to *semantical inconsistencies* - for details see again [Štuller, 1998] ) .

Here, to obtain meaningful results, we must be even more careful to semantically justify the meaning of performing the operation of the  $\pi$  - union .

## 2.2 Resume

We have seen that the integration of databases by unions may lead to (different types of the) inconsistencies .

*In order to eliminate as much as possible the occurrences of these inconsistencies one should try to*, especially in the case of the validity of the conditions **A3** &

- **A4** : *clear the databases* to be integrated from :
  - **incorrect data** which *can lead to data inconsistencies*
  - **incorrect integrity constraints** which *can lead to integrity constraints inconsistencies*
- **A5** : *semantically deeply analyze the corresponding attributes* in the relations to be integrated by  $\pi$  - unions .  
Missing to do so can lead to the *semantical inconsistencies*.

### 3 Integration by the Joins

We will illustrate the situation with the integration by joining the relations in the following examples .

*Example 1*

$R_1$	
Husband	Wife
Joseph	Mary

$R_2$	
Mother	Child
Mary	Jesus

$R = R_1 *_{Wife=Mother} R_2$		
Husband	Wife	Child
Joseph	Mary	Jesus

The comparison of the join with the  $\pi$  - union of the (same) relations :

$R = R_1 \cup_{\pi} R_2$	
Man	Woman
Jesus	Mary
Joseph	Mary

shows that the integration by joins against the integration by unions :

- allows **new relationships between objects** (entities or their attributes) which
- can be the sources of **new semantical inconsistencies**  
 ( having for arguments some of such new relationships )  
 in addition to the inconsistencies known from the unions .

Nevertheless, depending on the every concrete situation one must choose the best appropriate operation to perform the integration of the databases.



Example 2

$R_1$	
Mother	Son
Eve	John

$R_2$	
Mother	Daughter
Eve	Anne

$R = R_1 * R_2$		
Mother	Son	Daughter
Eve	John	Anne

$R = R_1 \cup_{\pi} R_2$	
Mother	Child
Eve	John
Eve	Anne

But in general what was said about the importance of the semantical justification for the  $\pi$  - union hold even more for the joins as the only condition on  $p$  relations  $R^{i_k}_{q_k}$  to be joinable is :

$$\mathbf{A6} : \quad \bigcap_{i=1}^p D^{i_k}_{q_k} (\pi^{i_k}_{q_k} (B^{i_k}_{q_k})) \neq \emptyset \quad ( B^{i_k}_{q_k} \subset A^{i_k}_{q_k} ) ( \forall k \in \hat{p} )$$

which is equal to the condition **A5** with the unique difference that  $B^{i_k}_{q_k} \subset A^{i_k}_{q_k}$  and so one can have in principle  $\prod_{i=1}^p 2^{|A^{i_k}_{q_k}|}$  possibilities of performing the join of  $p$  relations.

### 3.1 Resume

The integration of databases by joins may lead to similar types of the inconsistencies as in the case of the integration by unions.

*In order to eliminate as much as possible the occurrences of these inconsistencies one should try to*, especially in the case of the validity of the condition **A6**

- *clear the databases to be integrated from :*
  - **incorrect data** which *can lead to data inconsistencies*
  - **incorrect integrity constraints** which *can lead to integrity constraints inconsistencies*
- *semantically deeply analyze the corresponding attributes in the relations to be integrated by joins .*  
Missing to do so can lead to the *semantical inconsistencies*.

## 4 Other Operations of the Relational Algebra

All the other usual operations, except the compositions, do not contribute to the process of the integrations of databases. As concerns the different compositions, they are always expressible by joins (and projections) and so need not to be threatened again.

## 5 Conclusion

We have find *four* conditions **A3**, **A4**, **A5** and **A6** under which can occur different types of the inconsistencies in the process of the integration of databases.

The conditions **A3**, **A4**, **A5** apply to the integration by unions while the conditions **A6** applies to the integrations by joins.

The process of the integration of databases has been studied from mid-eighties, with the emphasis on the schema integration (see e.i. [Batini et al., 1986] as one of the first papers and [Ramesh & Ram, 1997] - [Santucci, 1998] as ones of the last ones) and with less attention on the integration of data themselves (see for instance [Orlowska, 1997]). To our knowledge none of them studied the existence conditions of the inconsistencies in the process of databases integration.

In the future we would like to further develop our ideas about the inconsistencies in databases integration with the focus to the possibilities of designing some kind of support for the resolution of these inconsistencies.

## 6 Appendix

### Definition

A **relation** in the RMD will be any triple  $\langle A, D, T \rangle$  with

1.  $A$  being a finite set of **attribute names** .
2.  $D$  being a mapping which maps every attribute name  $a \in A$  to a **domain** , noted  $D(a)$  .

Let us : *denote* by  $D(A)$  the *union* of all  $D(a)$  and *call* it the **universe of discourse** ( of the relation ) .

3.  $T$  being a finite set of **mappings**  $t$  from  $A$  to the universe of discourse  $D(A)$  such that  $t(a) \in D(a)$  for all  $a \in A$  .

### Notation 1

$$\widehat{m} = \{1, 2, \dots, m\} \quad (\widehat{\emptyset} = \emptyset)$$

### Notation 2

The *cardinality* of a set  $A$  will be denoted by  $|A|$  .

### Definition

Let  $R = \langle A, D, T \rangle$  be a relation and  $A_1 \subset A$  .

The **projection** of the relation  $R$  over  $A_1$  is the relation noted  $\mathbf{R}[A_1] = \langle A_1, D_1, T_1 \rangle$  such that :

1.  $D_1 = D/A_1$   
( the *restriction* of the mapping  $D$  on the subset  $A_1$  of  $A$  )
2.  $T_1 = T[A_1]$

### Notation 3

$$\mathbf{T}[A_1] = \{ t : A_1 \rightarrow D_1(A_1) \mid (\exists u \in T) (t(A_1) = u(A_1)) \}$$

### Notation 4

$$\begin{aligned} \text{Let } A_i &= \{a_{ij} \mid j \in |\widehat{A}_i|\} , \quad i \in \{1, 2\} . \\ (\forall j \in |\widehat{A}_i|) & (D_1(a_{1j}) \cap D_2(a_{2\pi(j)}) \neq \emptyset) \\ (\pi \text{ being an appropriate permutation in } |\widehat{A}_i|) & \\ & \Updownarrow \\ D_1(A_1) \cap D_2(\pi(A_2)) & \neq \emptyset \end{aligned}$$

### Lemma

$$((D_1(A_1) \cap D_2(\pi(A_2))) \neq \emptyset) \Rightarrow (|A_1| = |A_2|)$$

### Definition

Let  $R_i = \langle A_i, D_i, T_i \rangle$ ,  $i \in \{1, 2\}$ , be two relations such that :

1.  $(\exists A_{21} \subset A_2) (|A_1| = |A_{21}|)$
2.  $D_1(A_1) \cap (D_2/A_{21})(\pi(A_{21})) \neq \emptyset$   
(  $\pi$  being an appropriate permutation )
3.  $T_1(A_1) \subset T_2[A_{21}](\pi(A_{21}))$

Then we will say that the relation  $R_1$  is a **subrelation** of the relation  $R_2$  — what we will note :  $\mathbf{R}_1 \subset \mathbf{R}_2$

## Definition

Let  $R_i = \langle A_i, D_i, T_i \rangle$  be  $m$  relations ( $m \geq 2$ ).

The  $\pi$  - **union** of relations  $R_i$  is the relation noted

$$\bigcup_{\pi}^m \mathbf{R}_i = \langle \mathbf{A}, \mathbf{D}, \mathbf{T} \rangle \text{ such that :}$$

1.  $\mathbf{D}(\mathbf{A}) \cap \left( \bigcap_{i=1}^m \mathbf{D}_i(\pi_i(\mathbf{A}_i)) \right) \neq \emptyset$
2.  $\mathbf{T} = \bigcup_{i=1}^m \mathbf{T}_i(\pi_i(\mathbf{A}_i))$

## Notation 5

$$\bigcup_{i=1}^m \mathbf{T}_i(\pi_i(\mathbf{A}_i)) = \{ t : A \rightarrow D(A) \mid ((\exists i \in \widehat{m})(\exists u_i \in T_i) \\ (u_i(\pi_i(A_i)) = t(A))) \}$$

## Convention

In the case of permutations  $\pi_i$  being *identities* we will omit the prefix  $\pi$  - and speak shortly only about the **union** and note it :

$$\bigcup_{i=1}^m \mathbf{R}_i \text{ .}$$

## Definition

Let  $R_i = \langle A_i, D_i, T_i \rangle$  be  $m$  relations ( $m \geq 2$ ) and

$$B_i \text{ } m \text{ sets of attributes such that : } B_i \subset A_i \quad (\forall i \in \widehat{m}) \\ \bigcap_{i=1}^m D_i(\pi_i(B_i)) \neq \emptyset \text{ .}$$

The **join** of the relations  $R_i$ , *according to the attributes (sets)  $B_i$ , with respect to the equality*, is the relation noted

$*_{\pi_1(B_1)=\pi_i(B_i)} \mathbf{R}_i = \langle \mathbf{A}, \mathbf{D}, \mathbf{T} \rangle$  where :

$$\left( \mathbf{A} = \bigcup_{i=1}^m \mathbf{A}_i \right) \wedge \left( \mathbf{D} = \bigcup_{i=1}^m \mathbf{D}_i \right) \wedge \left( \mathbf{T} = *_{\pi_1(B_1)=\pi_i(B_i)} \mathbf{T}_i \right)$$

## Notation 6

$$D(a_j) = \bigcup_{i=1}^m D_i(a_j) \text{ , } \forall j \in |\widehat{A}| \quad \left[ \mathbf{A} = \bigcup_{i=1}^m \mathbf{A}_i \right] \\ \Updownarrow \\ \mathbf{D} = \bigcup_{i=1}^m \mathbf{D}_i$$

## Notation 7

$$*_{\pi_1(B_1)=\pi_i(B_i)} \mathbf{T}_i = \{ t : A \rightarrow D(A) \mid ((\forall i \in \widehat{m})(\exists u_i \in T_i)) \\ ((t(A_j) = u_j(A_j)) \wedge \\ (u_1(\pi_1(B_1)) = u_i(\pi_i(B_i)))) \}$$

## Convention

In case of  $\pi_i$  being the identities, the equality of  $B_i$  and such that they are **maximal** (in *set inclusion* sense) with such a property, we will omit the *index*  $\pi_1(B_1)=\pi_i(B_i)$  by the  $*$  and call the join shortly the **natural join** of  $\mathbf{R}_i$  .

## Convention

We will call a set of attributes a **compound attribute** or even, shortly, only an **attribute** .

When such a set will have *exactly one* element, we will call it, whenever necessary, a **simple attribute** .

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