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## **Classification of the Inconsistencies in the Databases Integration**

Štuller, Július  
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**CLASSIFICATION OF THE  
INCONSISTENCIES IN THE DATABASES  
INTEGRATION**

Július ŠTULLER

Technical report No. 746

May 1998

Institute of Computer Science, Academy of Sciences of the Czech Republic  
Pod vodárenskou věží 2, 182 07 Prague 8, Czech Republic  
phone: (+42 2) 6605 3200 fax: (+42 2) 85 85 789  
e-mail: [stuller@uivt.cas.cz](mailto:stuller@uivt.cas.cz)  
<http://www.uivt.cas.cz/~stuller>

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**Abstract**

The technological progress in the areas of the hardware and the software, together with the general expansion of the computers to almost all human activities, make it easier to realize the integration of many already existing databases. Unfortunately the process of the integration of (existing) databases can be accompanied by many various difficulties and problems. One of them is surely the possible occurrence of the inconsistencies appearing in this process of the integration. In the report we propose a classification of certain of these inconsistencies.

**Keywords**

database systems, logic, incomplete information

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# 1 Introduction

The technological progress in the areas of the hardware, specially in the field of the (secondary) memories where the ever increasing capacities are paradoxaly in the last several years available at ever decreasing prices and smaller physical sizes, and the software, continuously more and more user friendly, efficient and cheaper, together with the general expansion of the computers to almost all human activities, make it easier to realize the integration of many already existing databases.

Every database can be seen, at least from the point of view of the logic, as a conjunction of different facts (and depending on the representation of these as data, information or knowledge, we can obtain either a classical database system, either an information system or even a kind of fashioned knowledge-base system) which leads naturally to the idea of representing such a database as a (formal) logic theory.

The states of such a database and the operations over such a database obey usually certain rules (so called integrity constraints in the database approach) which can again be expressed in the corresponding logic (for instance in the form of special axioms).

Unfortunately the process of the integration of (existing) databases (as an example see for instance the series of psycho-medical studies [Štuller, 1995a] & [Štuller, 1997a]) can be accompanied by many various difficulties and problems. One of them is surely the possible occurrence of the inconsistencies (in sense of the classical logic — see for instance [Štuller, 1995b] - [Štuller, 1995f]) appearing in this process of the integration of databases.

The inconsistencies in the integration of databases can occur at various levels and they can be of different types. In this paper we propose a certain classification of these inconsistencies.

## 2 Formulation of the Problem

We will study the problem of the inconsistencies in the integration of several databases under the following natural, at least from the point of view of the logic, assumption :

**A1** : *Each of the considered databases to be integrated has no inconsistencies ( when taken alone ) .*

Furthermore, for reasons of the simplification, and having in mind the current situation in the area of the database technologies where the **Codd relational data model** prevail, we will suppose that :

**A2** : *All the databases to be integrated are relational ones.*

### 3 The simplest case

Let  $\mathcal{B}_i$ ,  $i \in \{1, 2\}$ , be two databases, each consisting of one relation, say  $R_i = \langle A_i, D_i, T_i \rangle$ ,  $i \in \{1, 2\}$ , respectively.

( See Appendix for definitions and notations )

From all the usual relational operations (operators) the ones which can lead to any possible inconsistencies are :

- the *union* of the relations
- the *joins*
- and the corresponding *compositions*.

Let us start by the union ( we will use its generalized form from [Štuller, 1997b] ) :

#### Definition 1

Let  $R_i = \langle A_i, D_i, T_i \rangle$  be  $m$  relations ( $m \geq 2$ ) .

The  $\pi$  - **union** of relations  $R_i$  is the relation noted

$\bigcup_{\pi}^m R_i = \langle \mathbf{A}, \mathbf{D}, \mathbf{T} \rangle$  such that :

1.  $\mathbf{D}(\mathbf{A}) \cap \left( \bigcap_{i=1}^m D_i(\pi_i(\mathbf{A}_i)) \right) \neq \emptyset$
2.  $\mathbf{T} = \bigcup_{i=1}^m T_i(\pi_i(\mathbf{A}_i))$

*Convention 1* In the case of permutations  $\pi_i$  being *identities* we will omit the prefix  $\pi$  - and speak shortly only about the **union** and note it  $\bigcup_{i=1}^m R_i$  .

At first, again for the simplification, we will suppose relations  $R_i$  are defined over the same relational scheme  $\mathcal{S} = \langle \mathbf{A}, \mathbf{D} \rangle$ , that is :

1.  $A_i = A$
2.  $D_i = D$

*Example 1*

$R_1$	
Name	Position
Peter	researcher

$R_2$	
Name	Position
Peter	director

$R = R_1 \cup R_2$	
Name	Position
Peter	researcher
Peter	director

Even in this very simple example without any further supplementary information it is impossible to decide whether an inconsistency appeared in the process of the integration of databases. Such a supplementary information is in general expressed in so called *integrity constraint(s)*.

We will suppose that we have such an integrity constraint. Let it be the following:

*Every value of the attribute **Name** is associated with no more than one value of the attribute **Position**.* (A particular case of a so called functional dependency)

More formally :

$$(\forall u, v \in T)((t(\text{Name}) = u(\text{Name})) \Rightarrow (t(\text{Position}) = u(\text{Position})))$$

Let us denote by  $\mathfrak{S}$  the set of all the possible integrity constraints over given universe of discourse  $U = D(A)$  and by  $\mathbf{I}$  a subset of the set  $\mathfrak{S}$ .

Let us further denote by  $\mathcal{R}(\mathbf{I})$  the set of all the relations over given universe of discourse satisfying  $\mathbf{I}$ . It is obvious that the following holds in general :

**Lemma 1**

$$((\mathbf{R}_1 \in \mathcal{R}(\mathbf{I})) \wedge (\mathbf{R}_2 \in \mathcal{R}(\mathbf{I}))) \not\Rightarrow ((\mathbf{R}_1 \cup \mathbf{R}_2) \in \mathcal{R}(\mathbf{I}))$$

Returning to our example they are two possibilities :

- They are some erroneous data in at least one of the relations  $R_i$  :  
 $(\exists i \in \widehat{m})(\exists R_i = \langle A_i, D_i, T_i \rangle)(\exists t \in T_i)(t \text{ is "incorrect"})$   
 ( i.e. this  $t$  does not represent correctly a fact from the reality we are trying to capture in a database - relation  $R_i$  ; in our Example it could mean that either Peter is not a researcher or that he is not a director ... )
- All data are correct but at least one of the integrity constraints is wrong :  
 $(\exists i \in I)(i \text{ is "incorrect"})$   
 ( i.e. this  $i$  does not correctly reflect the reality we are trying to model ; in our Example it would mean that there could be more than one Position associated with one Name ... )

In both cases the incorrect items must be removed. Let us denote by :

- $\hat{\mathbf{R}}$  the subrelation of the relation  $\mathbf{R}$  containing all "incorrect" data :  
 $\hat{\mathbf{R}} = \langle A, D, \{ t : A \rightarrow D(A) \mid t \text{ is "incorrect"} \} \rangle$
- $\check{\mathbf{R}}$  the subrelation of the relation  $\mathbf{R}$  containing no "incorrect" data :  
 $\check{\mathbf{R}} = \mathbf{R} - \hat{\mathbf{R}}$
- $\hat{\mathbf{I}}$  the subset of the set  $\mathbf{I}$  containing all "incorrect" integrity constraints :  
 $\hat{\mathbf{I}} = \{ i \in I : i \text{ is "incorrect"} \}$
- $\check{\mathbf{I}}$  the subset of the set  $\mathbf{I}$  containing no "incorrect" integrity constraints :  
 $\check{\mathbf{I}} = \mathbf{I} - \hat{\mathbf{I}}$

In the first case, as the result of the "correction of the data", we obtain new relations ( without erroneous data )  $\check{R}_k$  and the new union  $\bigcup_{k=1}^m \check{R}_k$  .

In the second case, as the result of the "correction of the integrity constraints", we obtain new set of the integrity constraints  $\check{I}$  ( without wrong constraints ) .

## 4 Generalization

Next we will suppose the relations  $R_k$  are defined over such different relational schema  $S_k = \langle A_k, D_k \rangle$  that there exists an appropriate permutation  $\pi$  in  $|\widehat{A}_k|$  that the following holds :  $D_1(A_1) \cap D_2(\pi(A_2)) \neq \emptyset$

*Example 2*

$R_1$	
Name	Position
Peter	researcher

$R_2$	
Name	Function
Peter	director

  

$R = R_1 \cup_{\pi} R_2$	
Name	Post
Peter	researcher
Peter	director

The necessary prerequisite is the existence of the "appropriate" permutation  $\pi$  in  $|\widehat{A}_k|$  which must be semantically justifiable for the concrete databases – relations : In our *Example 2* we presuppose that the ( names of the ) attributes **Position** and **Function** are synonyms ( i.e. they are semantically equivalent ) .

If this is the case the same reasoning we used to the union of relations apply also to the  $\pi$  - union of the relations and so we can summarize :

### Definition 2

Let  $R_k$  be  $m$  relations we want to make an union over (  $m \geq 2$  ) ,  
 $I_k$  be  $m$  corresponding sets of the integrity constraints and  
 $I_{m+1}$  be the set of the integrity constraints corresponding  
to the  $\pi$  - union of the relations  $R_k$  such that

$$I = \bigcup_{k=1}^{m+1} I_k \text{ is ( logically ) consistent.}$$

We will call the inconsistencies in the  $\pi$  - union  $\bigcup_{k=1}^m R_k$  :

$$\begin{aligned} \text{data inconsistencies} &\Leftrightarrow (\exists k \in \widehat{m}) (\check{R}_k \neq R_k) \\ \text{integrity constraints inconsistencies} &\Leftrightarrow (\exists k \in \widehat{m+1}) (\check{I}_k \neq I_k) \\ \text{semantical inconsistencies} &\Leftrightarrow (\exists k \in \widehat{m}) (\pi_k \neq \text{Identity}) \end{aligned}$$



## 5 Joins

In the following we will study the properties of the joins in the process of the integration of the relational databases .

We will not need to study the properties of the corresponding compositions as they are expressible in joins (and projections).

Let us start by giving the definition of the simplest join (so called the *equi-join*) from [Stuller, 1997b] :

### Definition 3

Let  $R_i = \langle A_i, D_i, T_i \rangle$  be  $m$  relations ( $m \geq 2$ ) and  $B_i$  be  $m$  sets of attributes such that

$$((B_i \subset A_i)(\forall i \in \widehat{m})) \wedge (\bigcap_{i=1}^m D_i(\pi_i(B_i)) \neq \emptyset) .$$

The *join* of the relations  $R_i$  , according to the attributes sets  $B_i$  , with respect to the equality , is the relation noted

$*_{\pi_1(B_1)=\pi_i(B_i)} R_i = \langle \mathbf{A}, \mathbf{D}, \mathbf{T} \rangle$  where:

$$(\mathbf{A} = \bigcup_{i=1}^m \mathbf{A}_i) \wedge (\mathbf{D} = \bigcup_{i=1}^m \mathbf{D}_i) \wedge (\mathbf{T} = *_{\pi_1(B_1)=\pi_i(B_i)} \mathbf{T}_i)$$

### Convention 2

In case of  $\pi_i$  being the identities, the equality of  $B_i$  and such that they are *maximal* (in *set inclusion* sense) with such a property , we will omit the *index*  $\pi_1(B_1)=\pi_i(B_i)$  by the  $*$  and call the join the *natural join* of  $R_i$  .

### Example 3

$R_1$	
Husband	Wife
Joseph	Mary

$R_2$	
Mother	Child
Mary	Jesus

  

$R = R_1 * R_2$		
Father	Mother	Child
Joseph	Mary	Jesus

Again, as in the case of the union, even in this very simple example without any further supplementary information it is impossible to decide whether an inconsistency appeared in the process of the integration of databases.

And, analogically to the case of the  $\pi$  - union , we could obtain the same three classes of the inconsistencies : *semantical*, *integrity constraints* and *data* inconsistencies.

## 6 Conclusion

By analyzing some simple problems we have arrived at the sources of possible inconsistencies in the integration of databases and we have proposed a certain classification of these inconsistencies based on their sources.

The process of the integration of databases has been studied from mid-eighties, with the emphasis on the schema integration (see e.i. [Batini et al., 1986] as one of the first papers and [Ramesh & Ram, 1997] - [Santucci, 1998] as ones of the last ones) and with less attention on the integration of data themselves (see for instance [Orlowska et al., 1997]). To our knowledge none of them proposed any kind of classification of the inconsistencies in the process of databases integration.

In the future we would like to further develop our classification of the inconsistencies in databases integration with the focus to the possibilities of designing some kind of support for the resolution of these inconsistencies.

## 7 Appendix

### Definition

A **relation** in the RMD will be any triple  $\langle A, D, T \rangle$  with

1.  $A$  being a finite set of **attribute names** .
2.  $D$  being a mapping which maps every attribute name  $a \in A$  to a **domain** , noted  $D(a)$  .

Let us : *denote* by  $D(A)$  the *union* of all  $D(a)$  and *call* it the **universe of discourse** .

3.  $T$  being a finite set of **mappings**  $t$  from  $A$  to the universe of discourse  $D(A)$  such that  $t(a) \in D(a)$  for all  $a \in A$  .

### Notation 1

$$\widehat{m} = \{1, 2, \dots, m\} \quad (\widehat{0} = \emptyset)$$

### Notation 2

The *cardinality* of a set  $A$  will be denoted by  $|A|$  .

### Notation 3

$$\begin{aligned} \text{Let } A_i &= \{a_{ij} \mid j \in |\widehat{A}_i|\} , \quad i \in \{1, 2\} . \\ (\forall j \in |\widehat{A}_i|) & (D_1(a_{1j}) \cap D_2(a_{2\pi(j)}) \neq \emptyset) \\ (\pi \text{ being an appropriate permutation in } & |\widehat{A}_i|) \\ & \Downarrow \\ & D_1(A_1) \cap D_2(\pi(A_2)) \neq \emptyset \end{aligned}$$

### Lemma

$$((D_1(A_1) \cap D_2(\pi(A_2))) \neq \emptyset) \Rightarrow (|A_1| = |A_2|)$$

### Notation 4

$$\begin{aligned} T &= \{t : A \rightarrow D(A) \mid (\exists i \in \widehat{m})(\exists u_i \in T_i) \\ & \quad (u_i(\pi_i(A_i)) = t(A))\} \\ & \Downarrow \\ T &= \bigcup_{i=1}^m T_i(\pi_i(A_i)) \end{aligned}$$

## Definition

Let  $R = \langle A, D, T \rangle$  be a relation and  $A_1 \subset A$ .

The **projection** of the relation  $R$  over  $A_1$  is the relation noted  $\mathbf{R} [A_1] = \langle A_1, D_1, T_1 \rangle$  such that :

1.  $D_1 = D/A_1$   
( the *restriction* of the mapping  $D$  on the subset  $A_1$  of  $A$  )
2.  $T_1 = T [A_1]$

## Notation 5

$$\begin{aligned} T_1 &= \{ t : A_1 \rightarrow D_1(A_1) \mid (\exists u \in T) (t(A_1) = u(A_1)) \} \\ &\Downarrow \\ T_1 &= T [A_1] \end{aligned}$$

## Notation 6

$$\begin{aligned} D(a_j) &= \bigcup_{i=1}^m D_i(a_j) \quad , \quad \forall j \in |\widehat{A}| \quad [ \mathbf{A} = \bigcup_{i=1}^m \mathbf{A}_i ] \\ &\Downarrow \\ \mathbf{D} &= \bigcup_{i=1}^m \mathbf{D}_i \end{aligned}$$

## Definition

Let  $R_i = \langle A_i, D_i, T_i \rangle$ ,  $i \in \{1, 2\}$ , be two relations such that :

1.  $(\exists A_{21} \subset A_2) (|A_1| = |A_{21}|)$
2.  $D_1(A_1) \cap (D_2/A_{21})(\pi(A_{21})) \neq \emptyset$   
(  $\pi$  being an appropriate permutation )
3.  $T_1(A_1) \subset T_2[A_{21}](\pi(A_{21}))$

Then we will say that the relation  $R_1$  is a **subrelation** of the relation  $R_2$  — what we will note :  $\mathbf{R}_1 \subset \mathbf{R}_2$ .

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