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## WORKING PAPER SERIES 5

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# The Behavioural Equilibrium Exchange Rate of the Czech Koruna

Luboš Komárek and Martin Melecký \*

## Abstract

The behavioural equilibrium exchange rate (BEER) model of the Czech koruna is derived in this paper and estimated by three methods suitable for non-stationary time series. The potential determinants of the real equilibrium exchange rate considered are the productivity differential, the interest rate differential, the terms of trade, net foreign direct investment, net foreign assets, government consumption and the degree of openness. We find that the Czech koruna was on average undervalued over the period 1994 to 2004 by about 7 percent with respect to the estimated BEER. The significant determinants of the equilibrium exchange rate of the Czech koruna appear to be the productivity differential, the real interest rate differential, the terms of trade and net foreign direct investment.

**JEL Codes:** C52, C53, E58, E61, F31.

**Keywords:** Czech Republic, equilibrium exchange rate modelling, ERM II, exchange rate misalignments, time-series analysis.

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## Nontechnical Summary

The overall objective of this paper is to assess the behavioural equilibrium exchange rate (BEER) of the Czech koruna by means of different estimation methods. The BEER approach draws on the real interest parity, through which the real exchange rate can be connected to the fundamentals. The model specification includes the productivity differential, foreign direct investment, the terms of trade, openness, net foreign assets, government consumption and the real interest rate differential as potential fundamental determinants of the real exchange rate of the Czech koruna with respect to the euro (the Deutsche mark).

We use three estimation methods suitable for non-stationary time series to estimate the derived BEER model and check the robustness of the acquired estimates. These methods are: the dynamic ordinary least squares (DOLS) method, the auto-regressive distributed lag (ARDL) approach and the full-information maximum likelihood (FIML) method. The acquired estimates are then used to analyse the short-term and medium-term misalignments of the Czech koruna. The short-term misalignment is determined by the deviation of the *actual* real exchange rate from the estimated equilibrium real exchange rate given by the conditioning set of *actual* fundamentals. The medium-term misalignment is determined by the deviation of the *actual* real exchange rate from the estimated equilibrium real exchange rate based on the *sustainable* values of the fundamentals, which are obtained by applying some cyclical filter to the latter estimates.

We find that the Czech koruna was on average undervalued over the period 1994 to 2004 by about 7 percent with respect to its BEER estimate. According to our estimates, the periods of major undervaluations appeared at the end of 1996, at the beginning of 1998, and during 2001. The periods of major overvaluation then appeared about the beginning of 1997 and 1999, and at the beginning of 2003. One specification seems to be particularly robust, and we believe that it may become relevant in the context of the discussions about the central parity of the Czech koruna for the exchange rate mechanism (ERM II), which the prospective euro area members are required to enter.

## **1. Introduction**

Policy makers and market participants both have a strong interest in appropriate estimates of equilibrium exchange rates and their prospective movements. They also have a keen interest in understanding the determinants of the equilibrium exchange rate and the implied misalignments of the actual exchange rate. Overvalued or undervalued exchange rates induce suboptimal allocation of resources between importers and exporters. Additionally, an overvalued currency may lead to an unsustainable current account deficit, increasing external debt and the risk of possible speculative attacks (see e.g. Kaminski, Lizondo and Reinhart, 1997), with detrimental consequences for the economy. There is also a general belief that an overvalued currency leads to lower economic growth, but that an undervalued currency has an equivocal effect on growth (e.g. Razin and Collins, 1997).

The prospects of an undervalued or overvalued currency are one of the crucial policy problems faced by the new EU Member States, which are supposed to adopt the euro in the near future. The prospective euro area members are required to first enter the exchange rate mechanism, ERM II, which is a part of the Maastricht criteria on exchange rate stability, and subsequently announce their euro-locking rates. ECB (2003) recommends in its position documents related to ERM II participation that “... *the central rate should reflect the best possible assessment of the equilibrium exchange rate at the time of entry into the mechanism. This assessment should be based on a broad range of economic indicators and developments while also taking account of the market rate*”. In broad terms, the “equilibrium” exchange rate refers to the rate that is consistent with medium-term macroeconomic fundamentals. The medium term, usually defined as 2 to 6 years, is often chosen as a benchmark in order to assess the level towards which the actual exchange rate is meant to gravitate.

The overall objective of this paper is to assess the behavioural equilibrium exchange rate of the Czech koruna by means of different estimation methods. The paper is structured as follows. Section two provides a brief overview of alternative concepts of equilibrium exchange rates and derives the behavioural model of the equilibrium exchange rate for a transition country, which is later used to estimate the behavioural equilibrium exchange rate (BEER) of the Czech koruna. Section three discusses potential fundamental determinants of the real exchange rate of the Czech Republic which may play a significant role prior to joining the euro area. Section four includes a description of the constructed variables and their unit-root tests. Section five outlines the estimation methods employed. In section six, we carry out estimations of the BEER model for the Czech koruna. Section seven discusses the resulting BEER and permanent equilibrium exchange rate (PEER) misalignments. Section eight concludes.

## 2. EER Concepts and Outline of the BEER Model

### 2.1 Concepts of Equilibrium Exchange Rates

Analysis of the real equilibrium exchange rate can be divided into two main categories for which various terms and names are used – fundamental and behavioural analyses.<sup>1</sup> A common starting point for inference on the equilibrium exchange rate is to use the purchasing power parity approach. However, there is a strong consensus in the literature that PPP is not an appropriate measure for developing and transition economies. Countries in a catching-up process may experience a trend appreciation of the real exchange rate which the simple version of PPP does not account for.<sup>2</sup>

A medium-term concept of the equilibrium exchange rate (EER) useful for policy purposes is the fundamental equilibrium exchange rate (FEER) developed by Williamson (1994), which defines the EER as the real exchange rate that corresponds to simultaneous internal and external balances. The cornerstone of this approach is current account sustainability, i.e. the level of current account deficits/surpluses that match long-term capital inflows/outflows. However, the FEER approach needs a normative judgement regarding the size of long-term capital flows. Also, FEER estimates are usually derived from large-scale macroeconomic models or partial trade blocks of a given economy. To circumvent normativity and the use of large macro models, the macroeconomic balance (MB) approach, which has been sharpened and widely used by the IMF<sup>3</sup>, estimates directly the sustainable level of current account deficits (surpluses) based on the saving-and-investment balance. The capital enhanced equilibrium exchange rate (CHEER) relates the nominal exchange rate, price level and interest rates in the domestic and foreign country. According to MacDonald (2000), the CHEER is a medium-run concept in the sense that it does not impose stock-flow consistency. Similar in spirit to these approaches is the NATREX (Natural Rate of Exchange) model advocated by Stein (1994) and Stein and Allen (1995), which is also based on the idea of concurrent internal and external balances. As opposed to FEER, it focuses on both the medium term and the long term. The long term is then the period during which the capital stock and foreign debt are assumed to converge to their steady-state values and the associated real exchange rate.

The behavioural equilibrium exchange rate (BEER) put forth by MacDonald (1997) and Clark and MacDonald (1998) draws on the real interest parity, through which the real exchange rate can be connected to the fundamentals. The permanent equilibrium exchange rate (PEER) is a variant of BEER which aims to decompose the estimated BEER into a permanent and transitory component (see Gonzalo and Granger, 1995), with the permanent component being interpreted as the equilibrium exchange rate (see Clark and MacDonald, 2000). The latter two approaches constitute

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<sup>1</sup> For further discussion, see e.g. Frait and Komárek (1999, 2001).

<sup>2</sup> A well-known phenomenon explaining trend appreciation is the Balassa–Samuelson effect, which is based on market-based non-tradable price inflation driven by fast productivity gains. However, there are two other factors that can contribute to trend appreciation of the real exchange rate: (i) trend appreciation of the tradable price-based real exchange rate, for example due to improvements in the terms of trade; (ii) administered/regulated price changes. For more detail, see Égert and Lommatzsch (2003) and Égert (2003).

<sup>3</sup> See Isard and Faruquee (1998) for an overview.



a focal point in this paper and we use them to obtain estimates of the real equilibrium exchange rate of the Czech koruna.

## 2.2 Outline of the BEER Model of the Czech Koruna

We start building the BEER model for the Czech koruna using the equation for the actual real exchange rate based on real uncovered interest parity (UIP):

$$q_t = E_t(q_{t+k}) - (r_t - r_t^*) + \omega_t \quad (1)$$

where  $q_t$  is the actual real exchange rate (RER),  $r_t$  and  $r_t^*$  are the domestic and foreign real interest rates with maturity  $t + k$ ,  $E_t(q_{t+k})$  is the conditional expectation of the  $t + k$  period real exchange rate and  $\omega_t$  is the time-varying risk premium. Further,  $r_t = i_t - E_t(\pi_{t+k})$ , is the *ex ante* real interest rate, where  $i_t$  is the nominal interest rate with maturity  $t + k$  and  $E_t(\pi_{t+k})$  is the conditional expectation of inflation,  $\pi_t$ , in period  $t + k$ . An increase in the risk premium  $\omega_t$  is deemed to induce a depreciation of the RER, which, given the model structure, generates an expected appreciation. The risk premium can be written out in full as:

$$\omega_t = \mu + \lambda_t + e_t \quad (2)$$

where  $\mu$  is a constant,  $\lambda_t$  is some proxy for the unobserved risk premium and  $e_t$  is a white noise process. Following Clark and McDonald (1998) the proxy is assumed to be a positive function of the relative fiscal stance  $fs_t / fs_t^*$ :

$$\lambda_t = f^+(fs_t / fs_t^*) \quad (3)$$

Hereafter the function  $f(\cdot)$  is restricted to be linear. For instance, an increase in the relative supply of the outstanding domestic debt increases the risk premium on the domestic currency and induces a depreciation of the current real exchange rate.

Now, consider again equation (1). The conditional expectation is also restricted to be a linear function of the information set we will condition upon. It is convenient at this point to elaborate on the conditional expectation of the  $t + k$  period RER, given that we are dealing with some specifics related to an economy in transition. For this reason, let us decompose the expectation into two parts:

$$E(q_{t+k} | I_t) = E(q_{t+k} | I_t^*) + E(q_{t+k} | I_t^T) \quad (4)$$

where  $I_t^*$  involves the traditional determinants of the RERs of developed economies (see e.g. McDonald, 1997), and  $I_t^T$  is a set of determinants that are effective only during transition periods and their effect on the RER ceases to be significant as the countries accomplish their transitions (convergence to developed economies). Applying the assumption of linearity and using equations (2)–(4), (1) can be expressed as:

$$q_t = \mu + \theta_1 X_{1,t} + \theta_2 X_{2,t} + \theta_3 (r_t - r_t^*) + \theta_4 (fs_t - fs_t^*) + e_t \quad (5)$$

where  $X_{1,t}$  is a subset of  $I_t^*$  and similarly  $X_{2,t}$  is a subset of  $I_t^T$ ,  $\theta_1$  is expected to be non-zero,  $\theta_2 \rightarrow 0$  as  $t$  approaches the end of the transition period,  $\theta_3$  is expected to be equal to negative one if the real UIP holds, and  $\theta_4$  is expected to be positive.

### 3. Fundamental Determinants of the EER

Appendix 1 provides an overview of the empirical findings concerning the significant determinants of the real exchange rates of the new EU Member States. Labour productivity or a proxy of it appears to enter the real exchange rate equation almost every time. There is strong evidence that an increase in productivity leads to an appreciation of the real exchange rate. However, the empirical findings on the signs of the other variables are mixed. Approximately one third of the papers find that government expenditure, the degree of openness, net foreign assets, the foreign real interest rate or the real interest differential, and the terms of trade have a significant impact on the real exchange rates of the new EU Member States. In addition, some other variables such as foreign debt, private expenditure, investment and regulated prices seem to have a significant influence on the real exchange rate. The mixed results with regard to some variables are attributable to the different time horizons considered and the methodologies applied in particular studies.

Hence, the set of possible exchange rate determinants associated with the BEER approach is quite broad. We try to choose those which from the theoretical and empirical points of view might be the most relevant for the Czech Republic<sup>4</sup> and comply with our constraint on data availability. We thus choose to consider the productivity differential, the terms of trade, foreign direct investment, the degree of openness, net foreign assets, government consumption and the real interest rate differential as the potential determinants of the EER for the Czech Republic. We discuss expected influences of the determinants on the EER with regard to the time horizons (short-, medium-, or long-run effects), sector composition (exchange rate pressures due to different development in tradable compared to non-tradable sectors in the domestic and foreign economy) and origin (domestic versus external) of the factors. A negative (positive) sign means that an increase in an explanatory variable is expected to induce an appreciation (depreciation) of the real exchange rate.

#### *Productivity Differential (-)*

A higher average productivity in the domestic relative to the foreign economy is typically expected to result in an appreciation of the domestic currency, mainly due to higher domestic inflation as a result of faster productivity growth. This channel is traditionally associated with the Balassa–Samuelson effect. Assuming perfect labour mobility, the latter effect tells us that if the productivity growth in the domestic tradable sector (manufacturing) is relatively higher than in the non-tradable sector (services), wages in the tradable sector tend to increase. The perfect labour mobility equalizes wages in the two sectors and increases the prices of non-tradable goods, hence increasing the overall price level in the domestic economy with respect to the foreign economy.

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<sup>4</sup> These determinants are similar for the other new Member States of the EU.

The appreciation can, however, materialize through the nominal exchange rate as well, as the increase in productivity implies higher economic growth and higher demand for the domestic currency relative to the foreign currency.

### ***Terms of Trade (-)***

A positive shock to the terms of trade, e.g. an increase in prices of exported goods, is assumed to generate two effects. A *substitution effect*, where the domestic production sector shifts production towards tradable (exportable) goods, resulting in higher wages in the tradable sector relative to the non-tradable sector. Wages subsequently equalize, due to sufficient labour mobility, inducing an increase in the overall domestic price level. The improvement in the current account and the higher domestic price level make the domestic currency appreciate. The *income effect*, on the other hand, comes about as the improvement in the trade balance raises the income of the domestic economy and higher demand for non-tradable goods emerges. To restore the internal equilibrium the real exchange rate is required to depreciate. The relative magnitudes of the substitution and income effects hinge on the relative price elasticity of the demands for imports and exports.

### ***Net Foreign Assets (-)***

The balance-of-payment logic postulates that current account deficits accumulate net foreign liabilities, with associated dividends and rental payments. The interest has to be paid for by an improvement in the trade balance. This requires the currency to depreciate, thus increasing the international price competitiveness of the country's exports. The portfolio balance reasoning suggests a similar adjustment of the real exchange rate. The country's debt resulting from the current account deficits has to be financed by internationally diversifying investors. To adjust their portfolios in the desired way they require a higher yield. With given interest rates, the higher yield is achieved through an expected appreciation of the debtor country's currency. This may require contemporaneous depreciation of the currency.

### ***Degree of Openness (ambiguous)***

A relatively higher degree of openness predisposes a given country to more efficient transfers of knowledge and technology in either direct or indirect form. It also enables the country to benefit from its comparative advantages to a higher degree. One can also argue that country risk is positively related to the degree of openness, since the country would suffer a significant loss by losing its international connections. This variable can be viewed as corresponding to the transition component of the real exchange rate dynamics, since one would expect a developed country to experience only limited variation in its degree of openness.

### ***Foreign Direct Investment (-)***

FDI inflow is expected to increase average productivity and eventually result in an appreciation of the domestic currency. The effect of FDI through the financial account works along the same lines. Specifically, the higher supply of foreign currency as a consequence of the FDI inflow induces a nominal appreciation of the domestic currency. In the long run, however, the current

account deficit resulting from the factor payments on the productive FDI makes the currency depreciate as the debt grows. This variable has a substantial effect on the development of the real exchange rate in emerging market economies, where the FDI flows are indeed substantial.

#### ***Real Interest Rate Differential (-)***

Inclusion of the real interest rate differential is well justified by the BEER approach, which derives the real exchange rate model from the underlying UIP that the real interest rate differential is a part of. According to UIP, a currency with a positive interest rate differential is expected to depreciate so as to equalize the yields in domestic and foreign currencies. The latter is required to eliminate any possible arbitrage opportunity. Similarly, an increasing interest rate differential induces portfolio reallocation and higher demand for the currency with the relatively higher interest rate. Both theories suggest that a positive interest rate differential with respect to the foreign currency should result in contemporaneous appreciation of the domestic currency.

#### ***Government Consumption (+)***

In the long run, the growing budget deficit could have a destabilizing effect on the economy and lead to a depreciation of the real exchange rate, assuming that Ricardian equivalence holds. In the short run, however, an increase in public consumption increases demand for non-tradable goods, due to the higher share of non-tradable goods in public consumption relative to private consumption. The higher demand for non-tradable goods induces higher prices of non-tradable goods, i.e. a higher overall domestic price level, and consequently an appreciation of the real exchange rate. The overall effect of this variable might thus be ambiguous.

## **4. Data Description and Unit Root Tests**

We use quarterly data covering the period from the first quarter of 1994 to the first quarter of 2004 (41 observations). The relevant series are seasonally adjusted by using the X12 procedure and the Tramo/Seats method. The dependent variable is the CPI-based real exchange rate. A description of the explanatory variables follows. Plots of all the series involved in the estimations are available in appendix 2.

The real exchange rate (*rer*) – the log of the nominal exchange rate index against DEM (EUR) deflated by the consumer price index (CPI) in the Czech Republic and in Germany. A decrease of this index denotes a real appreciation of the real exchange rate. Data source: IMF IFS database.

Productivity differential (*prod*) – the relative productivity differential in the Czech Republic and Germany calculated as the ratio of real GDP to employment in both countries. Data source: IMF IFS and Eurostat, New Cronos databases (seasonal adjustment by authors).

Foreign direct investment (*fdi*) – the four-quarter average of the ratio of net foreign direct investment to nominal GDP, both denominated in CZK. Data source: IMF IFS database (seasonal adjustment by authors).

Terms of trade (tot) – the ratio of export and import price indices. Data source: Eurostat, New Cronos database (seasonal adjustment by authors).

Openness (open) – the ratio of the sum of exports and imports to nominal GDP, all denominated in CZK. Data source: Eurostat, New Cronos database (seasonal adjustment by authors).

Net foreign assets (nfa) – the ratio of the negative of the net foreign assets of the banking sector to nominal GDP, both denominated in CZK. The negative of the net foreign assets of the banking sector is used to approximate the total NFA for the whole economy, as the latter series is not readily available for most CEE countries. Babetski and Égert (2005) find this approximation appropriate for the Czech economy. Data source: IMF IFS database (seasonal adjustment by authors).

Government consumption (gs) – total government consumption over nominal GDP was used as an approximation of the fiscal stance of the Czech Republic. Data source: IMF IFS and Eurostat, New Cronos databases (seasonal adjustment by authors).

Real interest rate differential (rird) – The differential between Czech and German lending rates deflated by Czech and German CPI inflation respectively. Data source: IMF IFS database.

We test for the order of integration of the series by employing the ADF-GLS test proposed by Elliott, Rothenberg and Stock (1996). This test improves on the low power of the conventional ADF test in finite samples by estimating the coefficients on the deterministic variables in the test specification prior to the estimation of the coefficient of interest. The results are reported in table 1:

**Table 1: Unit Root Tests**

Variable		Unit root test DF-GLS
rer	<i>Levels</i>	-2.5991 [c,t]
	<i>1<sup>st</sup> diff</i>	-4.7170 [c]***
prod	<i>Levels</i>	-2.0161 [c,t]
	<i>1<sup>st</sup> diff</i>	-5.5330 [c]***
nfa	<i>Levels</i>	-1.6385 [c,t]
	<i>1<sup>st</sup> diff</i>	-3.8980 [c]***
open	<i>Levels</i>	-2.4506 [c,t]
	<i>1<sup>st</sup> diff</i>	-5.3263 [c]***
rird	<i>Levels</i>	-2.7543 [c]***
	<i>1<sup>st</sup> diff</i>	-4.6169 ***
gs	<i>Levels</i>	-1.0459 [c]
	<i>1<sup>st</sup> diff</i>	-5.7741 ***
tot	<i>Levels</i>	-2.7085 [c]***
	<i>1<sup>st</sup> diff</i>	-3.2450 ***

**Note:** c or t in square brackets represent the inclusion of a constant or a time trend in the regression underlying the test.

The variables *rer*, *prod*, *nfa* and *open* appear to be integrated to order I(1) and their underlying processes are expected to include both stochastic and deterministic trends. The *gs* variable is non-stationary, integrated to order I(1) and with no deterministic trend. Variables *rird* and *tot*, on the other hand, appear to be stationary, i.e. integrated to order I(0). As the LHS variable and most of the RHS variables appear to be non-stationary, we apply suitable estimation methods for non-stationary time series, which we describe in the next section.

## 5. Applied Estimation Methods

The co-integration analysis is carried out using three methods so as to ensure that the acquired estimates have some robustness. These methods are: the dynamic ordinary least squares (DOLS) method introduced by Saikonon (1991) and Stock and Watson (1993), the auto-regressive distributed lag (ARDL) approach due to Pesaran and Shin (1995, 1999), and the full-information maximum likelihood (FIML) method due to Johansen (1995). We briefly describe the setup of the estimations below.

### • Dynamic OLS

Since the variables in the model come from a system with possible endogenous relationships, the DOLS method takes account of this by using a two-sided filter which enables to treat all the explanatory variables as weakly exogenous. The following equation is then estimated by OLS:

$$y_t = \beta X_t + \sum_{j=-k_1}^{k_2} \gamma_j \Delta X_{t-j} + \varepsilon_t \quad (6)$$

where  $y_t$  is the dependent variable  $X_t$  is a vector of explanatory variables, and  $k_1$  and  $k_2$  denote the number of leads and lags respectively. The length order of the leads and lags is determined on the basis of some of the information criteria for the model selection. The presence of cointegration is assessed by testing the stationarity of the residuals  $\varepsilon_t$ . For the purposes of our estimation we set  $k_1$  to one and equal to  $k_2$ . This choice is determined by the small sample of observations available to us.

#### • ARDL method

The error correction form of the ARDL model is given by an equation where the dependent variable in first differences is regressed on the lagged values of the dependent and independent variables in levels and first differences.

$$\Delta y_t = \phi y_{t-1} + \beta X_{t-1} + \sum_{j=1}^p \delta_j \Delta y_{t-j} + \sum_{j=0}^l \gamma_{i,j} \Delta X_{t-j} + \varepsilon_t \quad (7)$$

where  $y_t$  is the endogenous variable and  $X_t$  is a vector of explanatory and deterministic variables. The disturbance term  $\varepsilon_t$  is assumed to be independently distributed and independent of the regressors, i.e.  $E(\varepsilon_t | X_t) = 0$ . Further, the underlying *ARDL* ( $p, l$ ) model is assumed to be stable, which ensures that  $\phi < 0$ , and thus there exists a long-run relationship between  $y_t$  and  $X_t$ , defined as:

$$y_t = -(\beta' / \phi) X_t + \eta_t \quad (8)$$

where  $\eta_t$  is a stationary process. The coefficient standard errors are then obtained using the familiar *delta method*.

#### • Johansen method

The aforementioned single-equation approaches do not enable us to test for the presence of more than one co-integrating vector. Therefore, the Johansen co-integration technique is used to determine the number of co-integrating vectors in a vector autoregression (VAR) framework. The max and trace statistics proposed by Johansen (see e.g. Johansen, 1995) are used in this respect. The familiar VAR representation is:

$$y_t = \sum_{i=1}^{l+1} A_i y_{t-i} + \psi D_t + v_t \quad (9)$$

which may be reparameterized into the VECM representation as:

$$\Delta y_t = \sum_{i=1}^l \Gamma_i \Delta y_{t-i} + \Pi y_{t-1} + \psi D_t + v_t \quad (10)$$

where  $y_t$  is a vector of endogenous variables within the system,  $D_t$  contains deterministic components and exogenous variables and  $v_t$  is assumed to have a mean of zero and be homoscedastic and serially uncorrelated. The order of the VAR is assumed finite to exclude moving average components, and the parameters  $A_i$ ,  $U_i$ ,  $\psi$ , and  $\Sigma$  (the covariance matrix of  $v_t$ ) are assumed constant.  $\Pi$  is interpreted as the matrix of long-run responses. If the data co-integrate,  $\Pi$  must be of reduced rank,  $r < n$ , where  $n$  is the number of variables in  $y_t$ .  $\Pi$  may be factored as  $\Pi = \alpha\beta'$  (see Johansen, 1995), where  $\beta$  and  $\alpha$  are  $n \times r$  matrices which give the co-integrating vectors (empirical long-run relationships) and associated adjustment matrix respectively.

Due to the small sample available to us, we consider a maximum of two lags in the lag-length selection process. It appears that both the Hannan–Quin and Bayesian information criteria suggest that this maximum of two lags is employed. Both criteria are weakly consistent in the case where the lag-length determination is carried out for non-stationary variables. We thus use VAR(2) for the Johansen procedure and a maximum of two lags for the ARDL method.

The Trace and Maximum-eigenvalue statistics for the VAR(2) system of the variables considered are reported in table 2:

**Table 2: Cointegration Rank Test**

Hypothesized No. of CE(s)	Eigenvalue	Trace Statistic	1% Critical Values	Max-Eigen. Statistic	1% Critical Values
$r = 0$	0.921581	211.2254*	133.57	96.73611*	51.57
$r \leq 1$	0.644727	114.4893*	103.18	39.32500	45.10
$r \leq 2$	0.513163	75.16430	76.07	27.35339	38.77
$r \leq 3$	0.484161	47.81091	54.46	25.15453	32.24
$r \leq 4$	0.278751	22.65638	35.65	12.41727	25.52
$r \leq 5$	0.176734	10.23912	20.04	7.390105	18.63
$r \leq 6$	0.072232	2.849013	6.65	2.849013	6.65

**Note:** \* denotes rejection of the hypothesis at the 1% level. All the variables considered are assumed to be potentially endogenous except for the terms of trade.

The Trace statistic indicates presence of two co-integrating vectors at the 1 percent significance level. On the other hand, the Maximum-Eigenvalue statistic indicates the presence of only one co-integrating vector within the system. We continue with the more conservative choice of one co-integrating vector, which is easily identified in our case by normalizing on the real exchange rate.

## 6. Estimation Results

The estimates of the model in equation (5) using all three outlined estimation methods are reported in table 3. We apply the general-to-specific approach to arrive at the parsimonious versions of the estimates provided in table 3.



**Table 3: Estimations of the BEER Model of the Czech Koruna**

Variable/Method	DOLS(1,1)	ARDL(1,0,0,2,1)	JOH(2)
prod	-4.4375 (1.9484)**	-3.7471 (0.5612)***	-2.1708 (0.7180)***
tot	-4.5947 (1.0861)***	-1.1531 (0.5188)**	-----
nfa	-2.1548 (0.7250)**	-----	-----
open	-4.1612 (1.0165)***	-----	-----
gs	-3.7155 (0.8643)***	-----	-----
rird	-----	0.0361 (0.0155)**	0.0256 (0.0107)**
fdi	-0.5991 (0.1685)***	-0.0980 (0.0274)***	-0.1692 (0.0368)***
constant	75.557 (19.5446)***	27.5557 (3.8185)***	15.276 (3.2295)***
Serial Correlation AR(4)	1.2965 [0.3487]	2.0673 [0.1140]	0.16288 [0.9204]
Normality	0.9089 [0.6348]	0.60211 [0.7400]	4.4839 [0.1063]
Heteroscedasticity	0.2896 [0.9641]	0.56566 [0.4570]	0.79672 [0.6710]

**Note:** \*, \*\*, \*\*\* stand for significance at the 10%, 5% and 1% level respectively. Standard errors are in parentheses. The probability level of the diagnostic tests is in square brackets.

All three model estimates satisfy the common diagnostic tests, given the results reported in the last three rows of table 3. According to the estimates from all three methods employed, an increase in the productivity differential between the Czech Republic and Germany results in an appreciation of the real exchange rate of the Czech koruna. An improvement in the terms of trade makes the Czech currency appreciate with respect to the euro (mark) in real terms. The significance of this effect is supported by the DOLS and ARDL estimates. An increase in net foreign assets causes real appreciation, in accordance with the underlying theory. However, a significantly negative coefficient estimate is only found using DOLS. The increasing degree of openness of the Czech economy appears to induce real appreciation of the Czech koruna. This result is, however, only significant in the case of DOLS. Similarly, increasing government consumption as a proportion of GDP results in appreciation of the koruna with respect to the euro (mark). Such an observation is made only when the DOLS method is applied.

The coefficient estimates attached to the real interest rate differential are significantly positive. This contradicts with the expected signs on the interest rate differential based on UIP as shown in the BEER-model derivation. Our result suggests that a positive interest differential with respect to

Germany forecasts future appreciation of the Czech koruna. The ARDL and JOH estimates suggest that the domestic currency depreciates in real terms against the euro (mark) at a rate equal to about 3 percent of the corresponding interest rate differential<sup>5</sup>. The effect of foreign direct investment on the real exchange rate is significant and consistent across all three methods, with slight variability in the estimates' magnitudes. It appears that an increase in the net FDI inflow to the Czech Republic results in a real appreciation of the koruna.

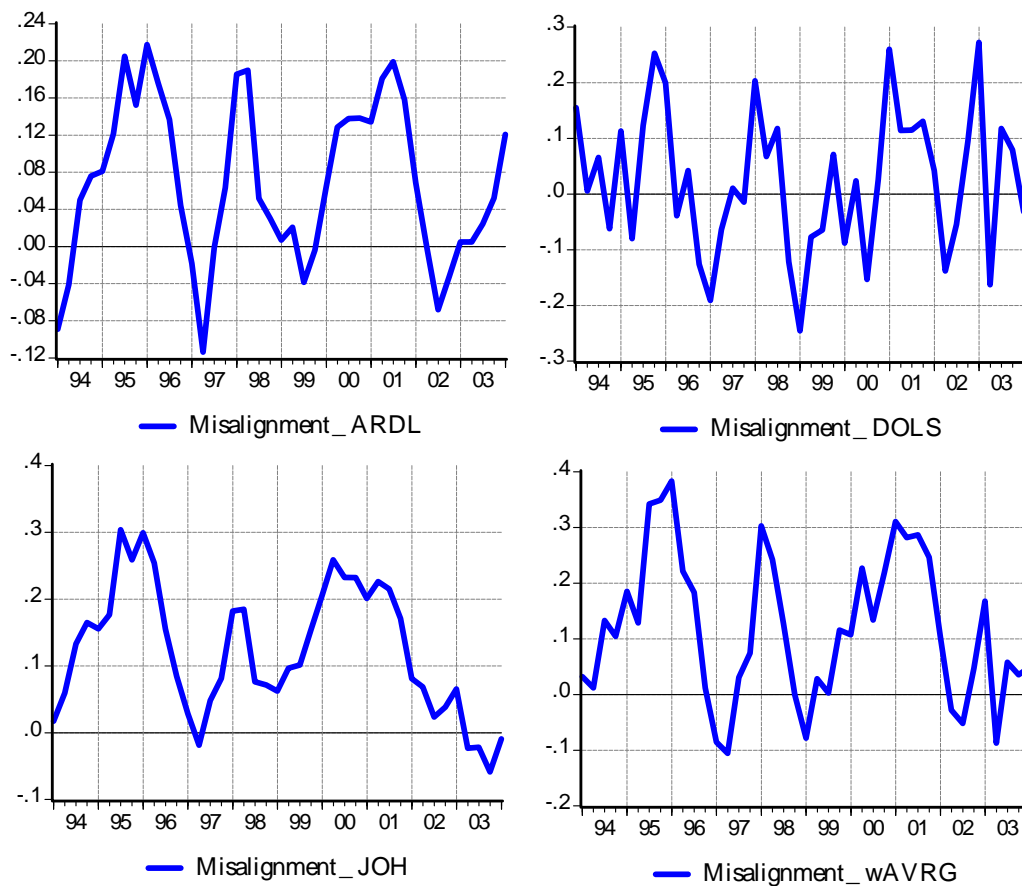
Even though all three estimation methods employed produce plausible results that satisfy the common diagnostic tests, one may want to rely on those that utilize more information than the others. This is especially appropriate in a case like ours, where the sample size is very small and the degree of parsimony of the general model specifications for each estimation method differs substantially. In our case, the ARDL estimates are favoured on such a premise. However, it is hard to judge the estimates of some of the unobserved (latent) variables just from the econometric point of view. It might be preferable to look at the economic rationale of the acquired estimates of the BEER. We do so in the next section within the discussion of the resulting misalignments of the real exchange rate of the Czech koruna.

## 7. Discussion of the Misalignments

When employing the behavioural approach it is possible to distinguish between two types of misalignments, i.e. deviations of the actual exchange rate from the estimates of its equilibrium values. The first deviation of interest is the current (*speculative*) misalignment, which is determined by the deviation of the *actual* real exchange rate from the estimated equilibrium real exchange rate given by the conditioning set of *actual* fundamentals. This misalignment measures the actual deviations from the equilibrium exchange rate of the Czech koruna in the short run. In figure 1 below, we present the short-run misalignments for the three estimation methods. In addition, we calculate a weighted average of the three misalignments where each misalignment is scaled according to its relative variance. A plot of this weighted average is also presented in figure 1.

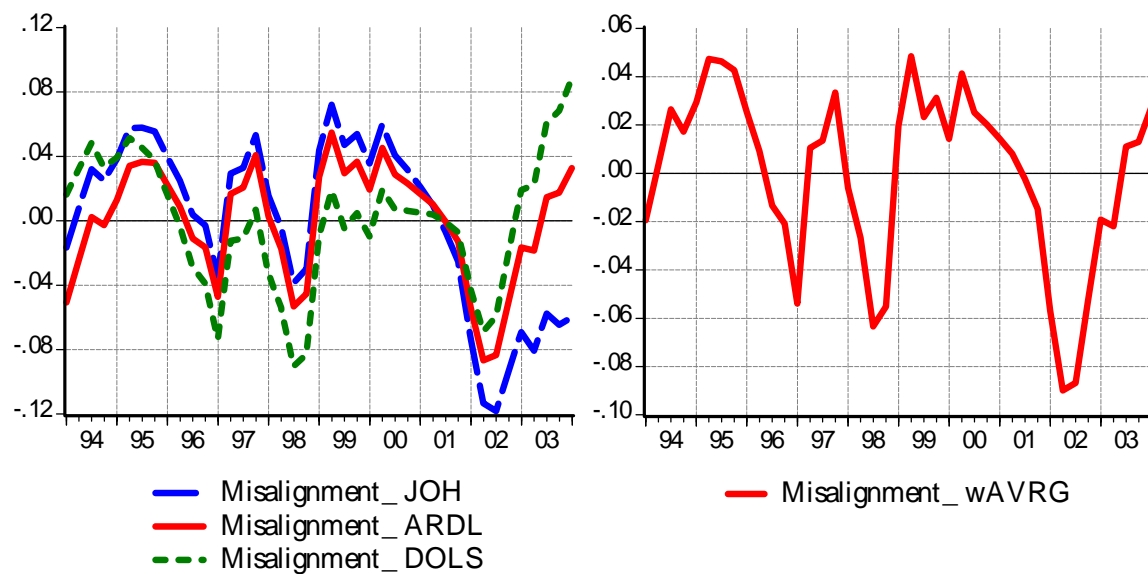
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<sup>5</sup> This contradictory coefficient estimate on the interest rate differential may bring about speculation that the positive risk premium vis-à-vis Germany (the euro zone) has been declining over the investigated period.

**Figure 1: Short-Run BEER Misalignment of the Czech Koruna**

The estimates of the BEER imply that the Czech koruna was on average undervalued over the period 1994 to 2004 by about 7 percent with respect to the short-run BEER. The highest average undervaluation is implied by the JOH estimates of about 12 percent. In general, the periods of major undervaluations appear to have happened at the end of 1996, at the beginning of 1998, and during 2001. The periods of major overvaluation then appeared around the beginning of 1997 and 1999, and at the beginning of 2003.

The second deviation of interest is the total (*cyclical* plus *speculative*) misalignment determined by the deviation of the *actual* real exchange rate from the estimated equilibrium real exchange rate based on the *sustainable* values of the fundamentals. The sustainable values of the estimated equilibrium exchange rate are obtained by applying some cyclical filter to the latter estimates, one example being the Hodrick–Prescott (HP) filter. We apply the HP filter to the quarterly estimates of the BEER according to the three estimation methods. The resulting misalignment then corresponds to the equilibrium exchange rate of the Czech koruna in the medium run. The medium-run misalignments of the Czech koruna are plotted in figure 2 (where we have imposed zero average undervaluation). The weighted average of the misalignments is also presented, again using the relative variances as the scaling factors.

**Figure 2: Medium-Run BEER Misalignment of the Czech Koruna**

The estimated PEER misalignments suggest that the major undervaluation periods took place during 1995 and from 1999 to the end of the first half of 2000. On the other hand, the major overvaluation emerged about the beginning of 1997, in mid 1998 and during 2002.

Next, we would like to test the economic rationale and information content of the implied misalignments by looking at their impacts on the dynamics of the real exchange rate. If the misalignment is well estimated it should contain considerable information about the future exchange rate dynamics. This intuition is captured by the following error-correction model:

$$\Delta q_t = \alpha(q_{t-1} - q_t^{BEER}) + \sum_{j=1}^{p_1} \delta_j \Delta q_{t-j} + \sum_{i=1}^{p_2} \gamma_i \Delta X_{t-i} + v_t \quad (11)$$

where  $q_t^{BEER}$  are the estimates of the BEER using DOLS, ARDL and JOH respectively. Except for the error-correction term  $q_{t-1} - q_t^{BEER}$ , we condition on the same information when estimating the error-correction models with the different estimates of  $q_t^{BEER}$  by OLS. Thus the model in which  $\alpha$  is most significant and delivers the highest R-squared or adjusted R-squared is likely to contain the most accurate estimation of the BEER of the Czech koruna. We report the estimates of the  $\alpha$  coefficients and the associated adjusted R-squares from the reduced error-correction models (the  $\Delta X_{t-i}$  are not considered when equation (11) is estimated) in table 4:

**Table 4 Estimates of the Reduced Error-Correction Models**

Coefficient/Model	$q_t^{BEER}$ by DOLS	$q_t^{BEER}$ by ARDL	$q_t^{BEER}$ by JOH
$\alpha$	-0.0825 (0.0316)**	-0.1733 (0.0391)***	-0.1033 (0.0275)***
Adj. R-squared	0.0748	0.2841	0.2075

**Note:** \*, \*\*, \*\*\* stand for significance at the 10%, 5% and 1% level respectively. Standard errors are in parentheses.

Since all the estimates of the  $\alpha$  coefficients are significant and negative all the BEER estimates follow correct economic rationale. Furthermore, according to the adjusted R-squares and the relative significance of the  $\alpha$  coefficients, the BEER estimated by the ARDL method conveys the most accurate information about the true real equilibrium exchange rate of the Czech koruna. The ARDL method uses the most parsimonious general model when it comes to estimation, produces estimates that satisfy all the applied diagnostic tests and provides the most informative estimates of the equilibrium exchange rate. As a result one may want to consider the fundamental determinants of the equilibrium ER proposed by this method in discussions about the prospective central parity of the Czech koruna for the ERM II.

## **8. Conclusion**

The primary objective of this paper was to analyse the misalignments of the real exchange rate of the Czech koruna using the behavioural equilibrium exchange rate model. We derive the BEER model of the Czech koruna along the lines of the BEER approach due to MacDonald (1997, 2000). This model is then used to analyse the short-term and medium-term misalignments of the Czech koruna. The initial model specification includes the productivity differential, foreign direct investment, the terms of trade, openness, net foreign assets, government consumption and the real interest rate differential as potential fundamental determinants of the real exchange rate of the Czech koruna with respect to the euro (the Deutsche mark). We use several estimation methods suitable for non-stationary time series to estimate the derived BEER model and check the robustness of the acquired estimates. We find that the Czech koruna was on average undervalued over the period 1994 to 2004 by about 7 percent with respect to its BEER estimate. According to our estimates, the periods of major undervaluations appeared at the end of 1996, at the beginning of 1998, and during 2001. The periods of major overvaluation then appeared about the beginning of 1997 and 1999, and at the beginning of 2003. The ARDL estimates of the equilibrium exchange rate seem to be the most preferable in our case and one may want to consider the significant determinants suggested by this estimation method in deliberations on the prospective central parity of the Czech koruna for the ERM II. These determinants are: the productivity differential, the real interest rate differential, the terms of trade and net foreign direct investment.

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## Appendix

### Appendix 1

#### *An Overview of RER Determinants Based on other Empirical Studies*

STUDY BY	PROD	GOV	OPEN	NFA	RIRD	TOT	INV	FD	PC	RP	FDI	No. variab.
Alberola (2003)	–			–/+								2
Alonso-Gamo et al. (2002)	–			+								2
Avallone and Lahrière-Révil (1999)	–	–	+			–			–			5
Begg et al. (1999)	–	–	–									3
Beguna (2002)		–	–			–					–	4
Bitans (2002)	–	+	+									3
Bitans and Tillers (2003)	–			–		+						3
Burgess et al. (2003)	–			+								3
Coricelli and Jazbec (2001)	–	–							–			3
Coudert (1999)	–							+				2
Csajbók (2003)	–	–	–	–	–	–						6
Darvas (2001)	–			–	–/+							3
De Broeck and Sløk (2001)	–		+									2
Dobrinsky (2003)	–	–										2
Égert and Lahrière-Révil (2003)	–											1
Égert and Lommatzsch (2003)	–		+		–			–/+		–		5
Filipozzi (2000)	–						–					2
Fischer (2002)	–	–			–/+	+						4
Frait and Komárek (1999, 2001)	–				+	–			(–)		–	4
Halpern and Wyplosz (1997)	–	–										2
Hinnosar et al. (2003)	–			–		–						3
IMF (1998)	–	+	–				+					4
Kazaks (2000)	–		+									2
Kim and Korhonen (2002)	–	–	+				–					4
Krajnyák and Zettelmeyer (1998)	–											1
Lommatzsch and Tober (2002b)	–			+	–							3
MacDonald and Wójcik (2002)	–			–/+	–					–		4
Maurin (2001)	–	–			–			+				4
Rahn (2003)	–			–								3
Randveer and Rell (2002)	–					–						2
Rawdanowicz (2003)	–				–	–						3
Rubaszek (2003)				–	–							2
Vetlov (2002)	–		+		+							3
Number of ‘–’	31	10	4	8	9	7	2	1	2	2	2	X
Number of ‘+’	0	2	7	5	3	2	1	3	0	0	0	X
Total number of studies	31	12	11	11	10	9	3	3	2	2	2	X

**Source:** Based on Égert (2003) and authors' update.

**Notes:** A (–) or (+) increase in the variable leads to an appreciation or depreciation of the real exchange rate respectively. *PROD* = productivity proxy; *GOV* = share of government consumption in GDP; *OPEN* = exports + imports over GDP; *NFA* = net foreign assets; *RIRD* = real interest rate differential; *TOT* = terms of trade = export prices / import prices; *INV* = share of investment in GDP; *FD* = foreign debt to GDP; *PC* = share of private consumption in GDP; *RP* = regulated prices (or differential vis-à-vis benchmark economy), *FDI* = foreign direct investment over GDP; *S* = national savings over GDP.



## **Appendix 1 - References**

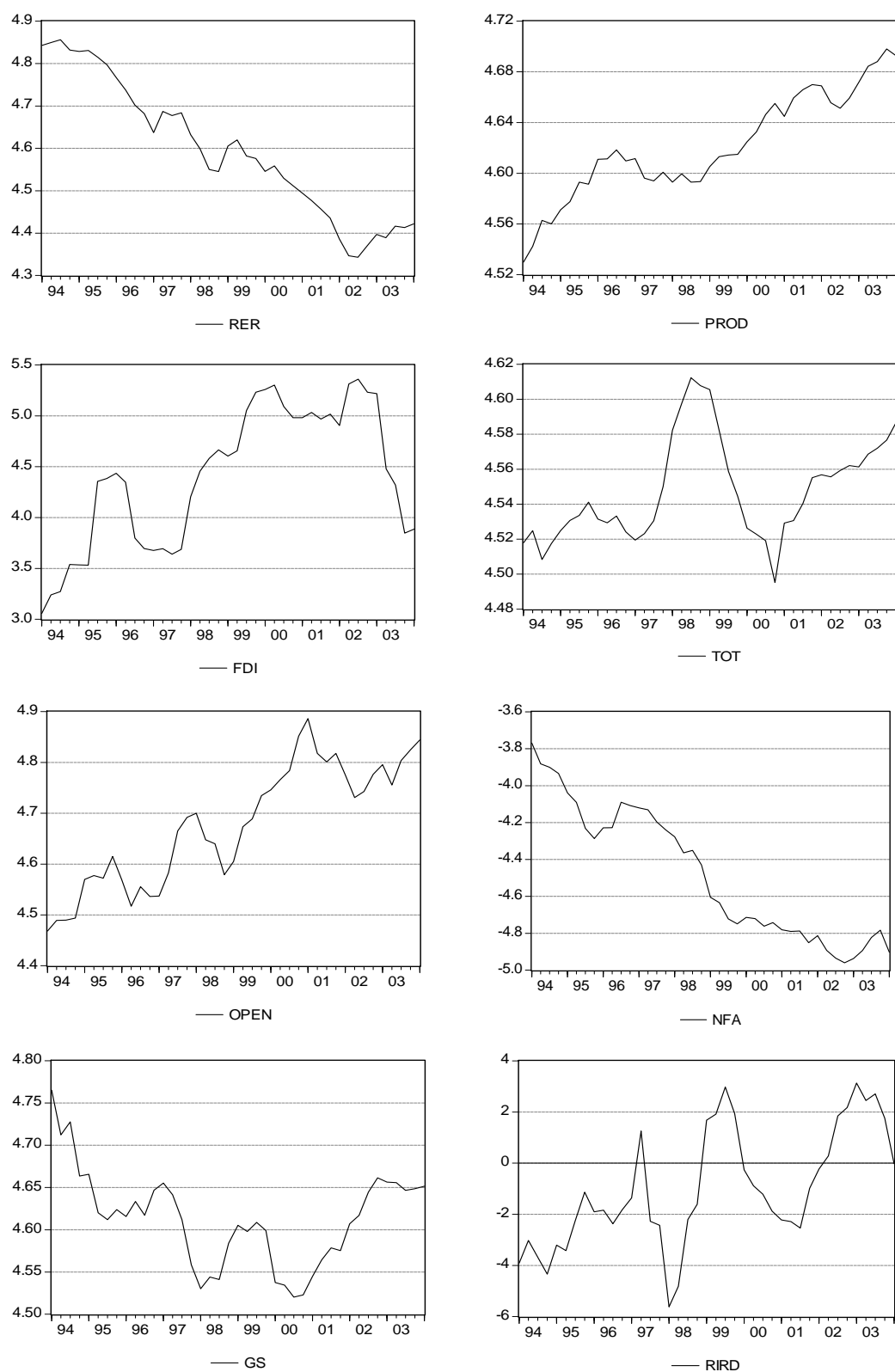
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## Appendix 2

### *Development of the Main Fundamental Determinants*



**Note:** variables presented in logarithms, except RIRD.

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